

DTU

22485 Medical Imaging Systems

Lecture 1, September 2024

Introduction to course and ultrasound physics

Jørgen Arendt Jensen
Department of Health Technology

$f(x+\Delta x) = \sum_{i=1}^n \frac{(\Delta x)^i}{i!} f^{(i)}(x)$


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Outline for Today

- Teachers
- Outline of course
 - Purpose
 - Course content and web-site
 - Books and notes
 - Exercises
- Medical ultrasound systems
 - History
 - Anatomic imaging
 - Blood flow imaging
 - Examples
- Physics of ultrasound after break



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Practical details

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Practical details – Teacher for lectures

- Jørgen Arendt Jensen
- DTU Health Technology
- Build 349, room 222
- Phone: 45 25 39 24
- E-mail: jaje@dtu.dk
- Web: home.healthtech.dtu.dk/jaj/
- Responsible for all practical details



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Practical details – Teacher for lectures



- Billy Yiu
- DTU Health Technology
- Build 349, room 232
- E-mail: yshyi@dtu.dk

- Handles part of the ultrasound, exercises and assignments

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Teacher for the MR part



- Hans Magnus Henrik Lundell

- DTU Health Technology
- Build 349, first floor
- E-mail: hmag@dtu.dk

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Guest lecturers



- Chief physicist, Cand.scient Søren Holm, Klinisk fysiologisk og nuklearmedicinsk klinik Rigshospitalet
- Professor, dr.med. Liselotte Højgaard, Klinisk fysiologisk og nuklearmedicinsk klinik Rigshospitalet
- Senior researcher, PhD Jakob Sauer Jørgensen, DTU Compute
- Senior Research Officer Carsten Gundlach, Department of Physics, DTU
- PhD, MD Thomas Kristensen, Diagnostisk Center, Radiologisk klinik afsnit 2023, Rigshospitalet
- Associate professor, PhD Borislav Tomov, DTU Health Technology
- PhD student, MD Nathalie Panduro, Rigshospitalet, Radiologisk Afdeling

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Practical details – Teachers for exercises



- PostDoc Lasse Thurmann Jørgensen

- DTU Health Technology
- Build 349, room 208
- E-mail: latjo@dtu.dk

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Practical details – Teachers for exercises



- PostDoc Lars Emil Haslund
- DTU Health Technology
- Build 349, room 224
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The purpose of the course is ...



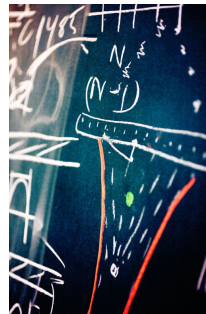
- to obtain a thorough understanding of diagnostic imaging systems
- to give an understanding of the relation between different medical imaging systems and other measurement systems
- to relate the physical measurement situation with the applied signal processing
- to give an understanding for "good" (robust/accurate/sensitive) measurement and processing methods
- to give an active knowledge of the signal and image processing in modern imaging systems through exercises and project assignments.

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Prerequisites for following the course

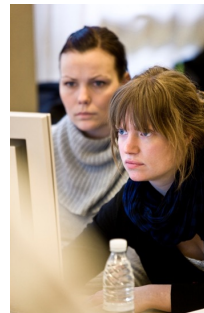


- Assumes that the curriculum in Medicine & Technology has been followed:
 - 22052/31610 Applied signal processing
 - 22481/31540 Introduction to medical imaging
 - Courses in human anatomy and physiology
 - Capable of programming in Matlab
 - Interest in Medical Imaging!



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Teaching paradigm



- Discussion of reading material each Monday (13-15) in aud. 23, build. 341 and Thursday (9-11) aud. 11, build. 308
 - Discussion of Chapter and **Cold-call**
 - **Discussion assignment of the day**
 - Questions
 - Slides to support discussion
 - Small assignments
 - Matlab demonstration
- Exercises some Mondays (15-17) in E-data bar build. 341 room 015 (check plan)
- Two final assignments with hand-in of reports. Oral exam about the reports, exercises, and reading material (everything counts!)

12/x

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Web-site and course plan

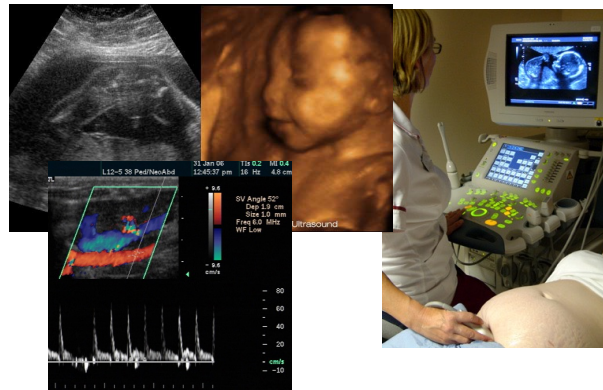
- Web-site at: courses.healthtech.dtu.dk/22485/
- Course plan in 4 themes:
 - Ultrasound imaging
 - X-ray and computer tomography (CT)
 - Radio isotopic imaging (PET, PET/CT, SPECT)
 - Magnetic resonance (MR)
- Slides are posted roughly 1 hour or less before the lecture
- All data and exercises can be found on the web site and on DTU Learn

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Modern Medical Imaging Systems

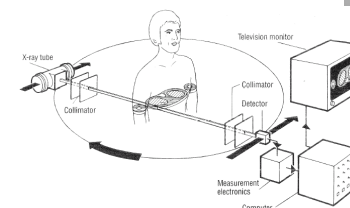


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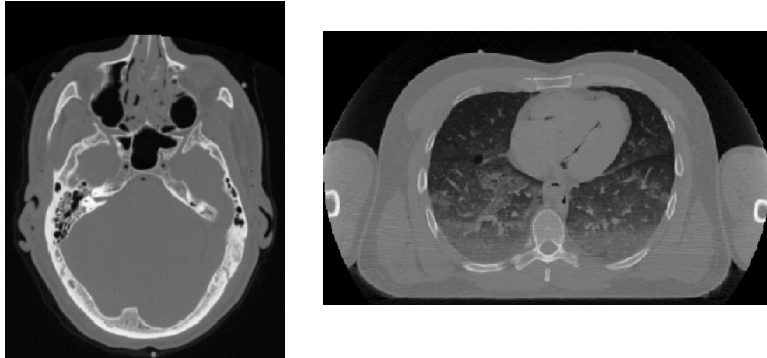
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CT scanning



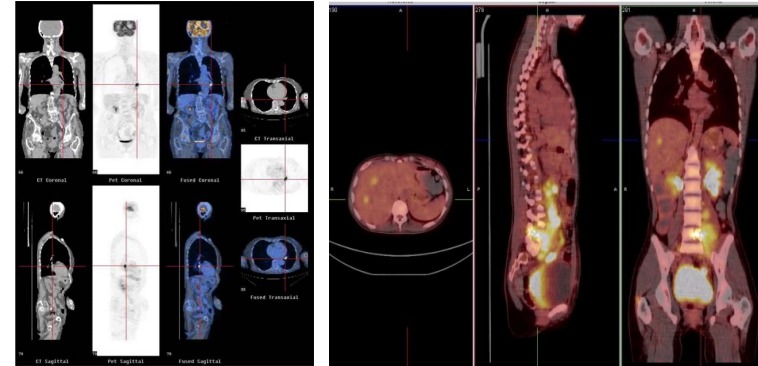
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CT scans



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Radio isotopic imaging (PET/CT images)



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Magnetic resonance (MR)



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Books



- Two books are used:

- [Jørgen Arendt Jensen: Estimation of Blood Velocities Using Ultrasound. A Signal Processing Approach. Cambridge University Press, 1996.](#)

(third edition August, 2013 can be downloaded from DTU Learn. Note this is copyrighted material; For your Eyes only!)

- P+L: J. L. Prince & J. M. Links: *Medical imaging signals and systems (second edition)*, Pearson Prentice Hall Bioengineering, 2015, ISBN: 978-0-13-214518-3 It can be bought from the PF bookstore with a discount. Is used from October 6.

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Exercises



- Seven exercises are made during the course
- Topics: Matlab programs for simulating the signal and image processing in medical imaging.
- Time: Monday 15-17 in the E-data bar, build. 341, ground floor room 015
- Made in groups of two (form groups today and Thursday)
- No reports hand-in, but you can be asked questions about it at the exam
- Lays the ground work for the two projects
- Prepare for the exercises!
- Tutors: Lasse Thurmann Jørgensen and Lars Emil Haslund

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Final assignments



- Two assignments are made:
 1. Ultrasound signal processing (hand in 28/10)
 2. Reconstruction and artefacts (hand in 5/12)
- Made in groups of two
- Evaluated with a grade that counts towards the final grade
- Hand-in time is strict
- Hand in as pdf and Urkund is used for plagiarism check

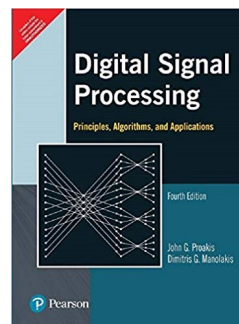
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Quiz on signal processing next time



Topics:

- What is the spectrum of a square wave?
- Basic rules for signals and correlation functions
- What is the spectrum of a sinusoidal pulse with M oscillations
 - Sketch the signal
 - Sketch the spectrum
- What is the autocorrelation of a white, random signal?
- How do you plot in Matlab
- Takes 15 min and we will discuss it next time Monday



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Medical Ultrasound: History and Systems

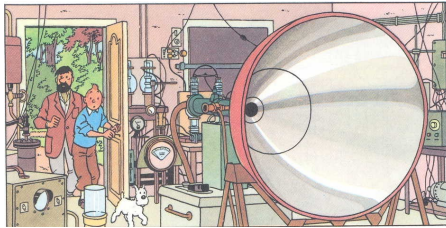


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What is ultrasound?



- Ultrasound: Pressure waves with frequencies higher than 20 kHz, i.e. higher than the audible range of man. Compared to X-rays and CT, ultrasound is harmless unless very high intensities are used.



Tintin and Captain Haddock discovers Tournesol's deadly ultrasound device.

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Ultrasound history

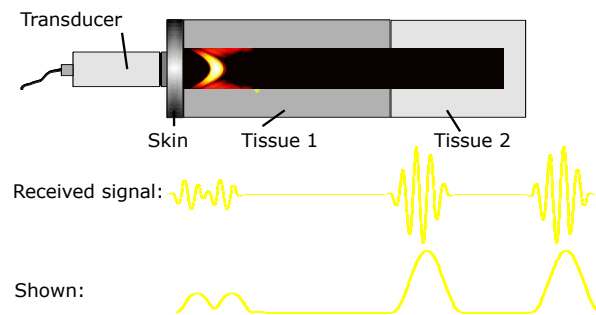


- Used for many years by animals – bats and dolphins
- Piezoelectric effect discovered by the Curie brothers in 1888
- High frequency pressure waves in water (SONAR) was developed after World War I to detect submarines.
- The first ultrasound systems for medical imaging was made in the 1950s, mainly by Howry and Wild.
- The first velocity estimation system by Satomura in Japan, 1957



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Pulse-echo principle for imaging



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Modern ultrasound system



- Speed of sound: 1540 m/s
- Time for one line is 200 μ s for a depth of 15 cm
- Can yield 5,000 lines per second
- One image consists of 100-200 lines
- Frame rate is 10-50 images/s
- Electronic arrays transducers with 192 elements are used



Modern ultrasound scanner
from B-K Medical

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B-mode system

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B-mode image of right liver lobe and kidney

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Example of ultrasound movie

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Medical Ultrasound: Blood velocity Estimation

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Doppler effect

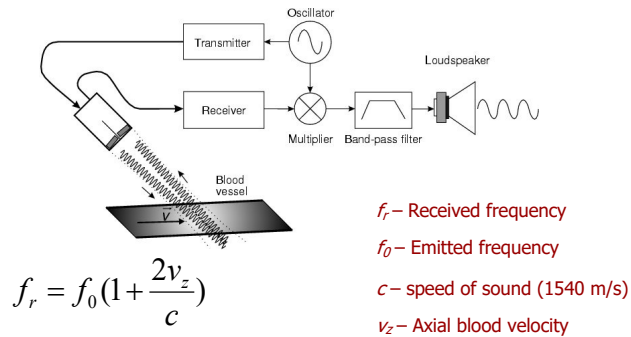
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$$f_r = f_0 \left(1 + \frac{v}{c}\right)$$

- f_r – Received frequency
- f_0 – Emitted frequency
- c – speed of sound (1540 m/s)
- v – Train velocity

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Velocity estimation system (Doppler system)



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Audio generation

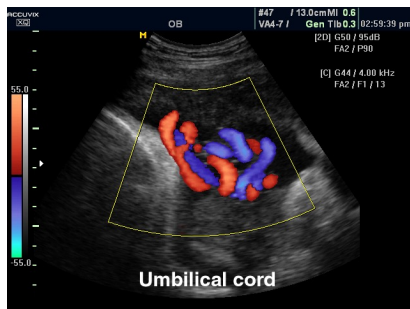
- Received and demodulated frequency is in the audio range:
 - Emitted frequency: 3-10 MHz
 - Blood velocity: 0-1 m/s
 - Resulting frequency example:

- Matlab example ([snd_demo](#))

$$f_{doppler} = \frac{2v_z}{c} f_0 = \frac{2 \cdot 0.75}{1540} 5 \cdot 10^6 = 5 \text{ kHz}$$

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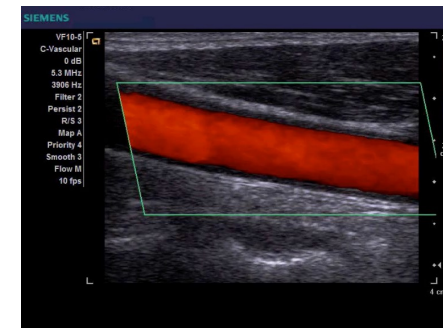
Color flow imaging (CFM)



- Ultrasound is emitted 8 to 16 times in the same direction
- The velocity is estimated along the image direction
- A blue color indicates velocity towards the transducer and red away
- Next slide is an example from the carotid artery and the jugular vein

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Modern color flow mapping

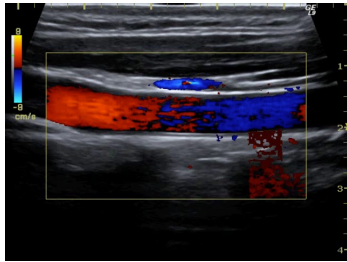


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Conventional velocity estimation system



- Low frame rate (approx. 20 Hz)
- Angle dependent velocity estimation



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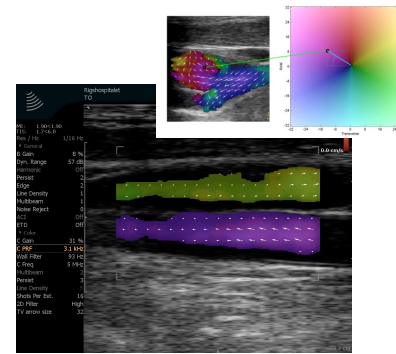
- Velocity changes direction in the image
- Determination is dependent on angle between beam and flow:

$$V_z = |v| \cos(\text{angle})$$

- At 45 degrees: 71% of velocity
- At 60 degrees: 50% of velocity
- At 80 degrees: 17% (!) of velocity
- At 90 degrees: 0%

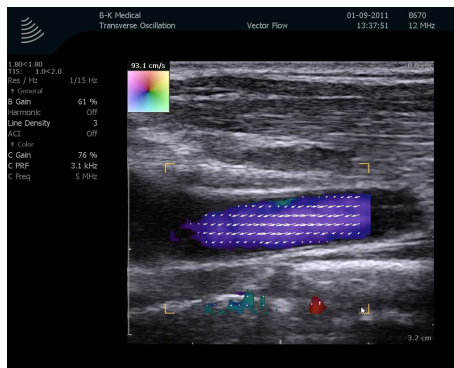
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DTU developed vector flow method: BK Medical ProFocus scanner FDA approved January 2012



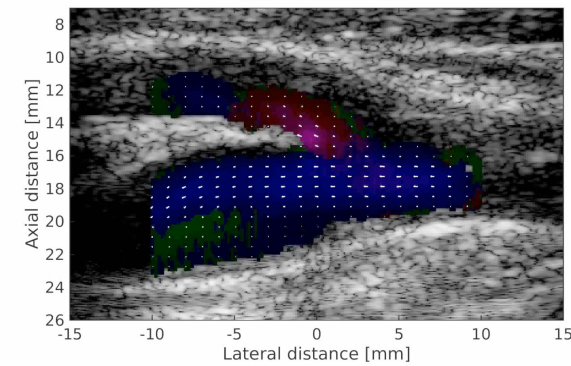
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Scanning of the carotid artery



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SA Vector Flow Imaging in Carotid bifurcation Frame Rate: 2000 Hz Time = 2.5852 sec



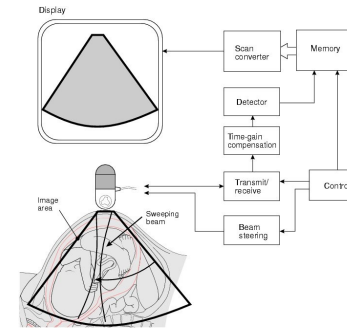
Villagomez et al, IUS 2015

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Medical Ultrasound: Physics

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Ultrasound and scanning



- Pulse emission
- Speed of sound $c=1540$ m/s in soft tissue
- Distance in tissue: $d = c \cdot t$
- Pulse send out:

$$p(t) = \sin(2\pi f_0 t) \quad 0 \leq t \leq \frac{M}{f_0}$$

- Wavelength:

$$T_0 = \frac{1}{f_0}, \quad \lambda = T_0 c = \frac{c}{f_0}$$

- Length of pulse = $M \lambda$

- Typical parameters:

$$f_0 = 5\text{MHz}, \quad \lambda = \frac{1540}{5 \cdot 10^6} = 0.3\text{mm}$$

$$M = 2 \Rightarrow M\lambda = 0.6\text{mm}$$

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Reflection

- Reflection of sound:

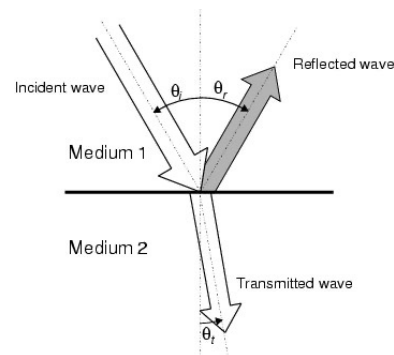
$$R_a = \frac{z_2 \cos \Theta_i - z_1 \cos \Theta_t}{z_2 \cos \Theta_i + z_1 \cos \Theta_t} = \frac{p_r}{p_i}$$

- Characteristic acoustic impedance: $z = \rho c$

- Snell's law: $\frac{c_1}{c_2} = \frac{\sin \Theta_i}{\sin \Theta_t}$

- Transmission of sound:

$$T_a = \frac{2z_2 \cos \Theta_i}{z_2 \cos \Theta_i + z_1 \cos \Theta_t} = \frac{p_t}{p_i}$$



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Table with characteristic acoustic impedances

Medium	Density kg/m ³	Speed of sound m/s	Characteristic acoustic impedance kg/[m ² ·s]
Air	1.2	333	0.4×10^3
Blood	1.06×10^3	1566	1.66×10^6
Bone	$1.38 - 1.81 \times 10^3$	2070 - 5350	$3.75 - 7.38 \times 10^6$
Brain	1.03×10^3	1505 - 1612	$1.55 - 1.66 \times 10^6$
Fat	0.92×10^3	1446	1.33×10^6
Kidney	1.04×10^3	1567	1.62×10^6
Lung	0.40×10^3	650	0.26×10^6
Liver	1.06×10^3	1566	1.66×10^6
Muscle	1.07×10^3	1542 - 1626	$1.65 - 1.74 \times 10^6$
Spleen	1.06×10^3	1566	1.66×10^6
Distilled water	1.00×10^3	1480	1.48×10^6

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What are the reflection coefficients?



- For normal incidence ($\theta_i = 0 = \theta_t$)

$$R_a = \frac{z_2 \cos \Theta_i - z_1 \cos \Theta_t}{z_2 \cos \Theta_i + z_1 \cos \Theta_t} = \frac{p_r}{p_i} = \frac{1 - \frac{z_1}{z_2}}{1 + \frac{z_1}{z_2}}$$

- Liver to fat?
- Bone to fat?
- Fat to air?
- Use the previous table to calculate the values.

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What are the reflection coefficients?



- Liver to fat? $z_1 = 1.66 \text{ MRayl}, z_2 = 1.33 \text{ MRayl}$



- Bone to fat? $z_1 = 7.38 \text{ MRayl}, z_2 = 1.33 \text{ MRayl}$

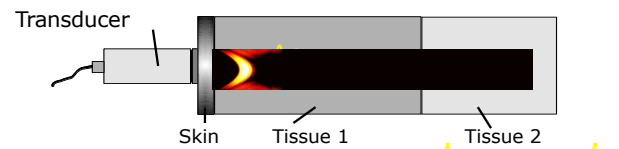


- Fat to air? $z_1 = 1.33 \text{ MRayl}, z_2 = 0.4 \text{ kRayl}$



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Reflection and reception

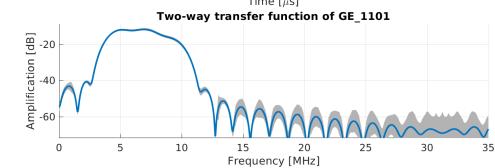
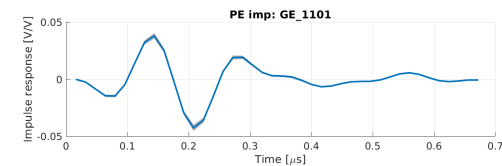


Depth-time relation: $2d = ct \Rightarrow t = \frac{2d}{c}$

For a number of reflections: $y(t) = r(t) * p(t)$ (Matlab con_demo)
Reflections Pulse

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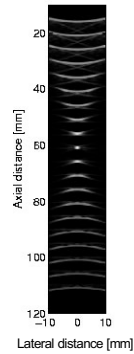
Measured ultrasound pulse



GE L8-18i-D, 8-18 MHz high frequency broadband transducer
 Center frequency around 8 MHz, B=7 MHz at -20 dB

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Resolution and point spread functions



- Resolution in the image is characterized by the point spread function (PSF)
- Spatially variant
- Axial resolution in depth
- Lateral resolution across ultrasound beam
- Azimuth – out of image plane
- Image model: $y(t) = r(t, \vec{r}) ** p(t, \vec{r})$
 - ** - 3D (spatial) convolution
 - r - Reflections
 - p - Point spread function

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Axial resolution



- Pulse emission
- Speed of sound $c=1540$ m/s in soft tissue
- Distance in tissue: $z = c \cdot t / 2$
- Pulse send out: $p(t) = \sin(2\pi f_0 t) \quad 0 \leq t \leq \frac{M}{f_0}$

• Axial resolution: $\frac{M}{f_0} \frac{c}{2} = \frac{M}{2} \lambda$

• Transducer bandwidth = f_0/M

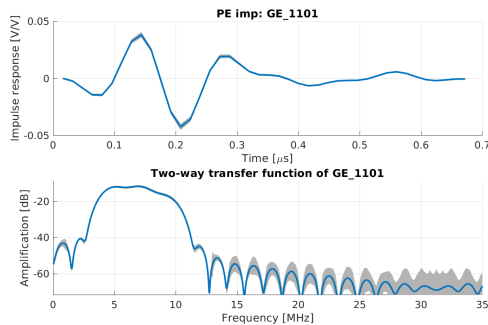
• Typical parameters: $f_0 = 5\text{MHz}, \lambda = \frac{1540}{5 \cdot 10^6} = 0.3\text{mm}$

$M = 2 \Rightarrow res \approx 0.3\text{mm}$

$T = \frac{M}{f_0} = \frac{2}{5 \cdot 10^6} = 0.4\mu\text{s}$

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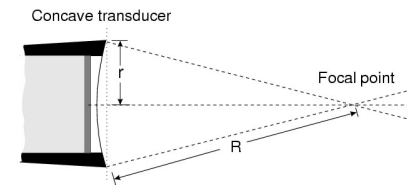
Measured ultrasound pulse



Transducer: $f_0=8$ MHz, $\lambda = 0.19$ mm, $B=7$ MHz at -20 dB
 Axial resolution: -6 dB: $0.125 \mu\text{s}$, $d=C T/2 = 1.54 \cdot 10^6 \times 0.125 \cdot 10^{-6}/2 = 0.096$ mm $\sim \lambda/2$

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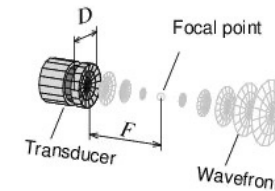
Lateral resolution



- Approximate resolution at focus at Full Width Half Max (FWHM, -6 dB):

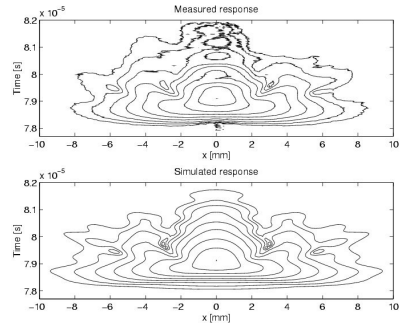
$$d_{3dB} = FWHM = \lambda \frac{R}{2r} = \lambda F_{\#}$$

$$F_{\#} = \frac{R}{2r} = \frac{F}{D} \quad \text{F-number (typically 1-5)}$$



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Point spread functions (measured and simulated)



PSF for concave 3 MHz transducer at 60 cm, diameter 2 cm, focus at 10 cm
6 dB between contours. Top - Measured, Bottom - Simulated

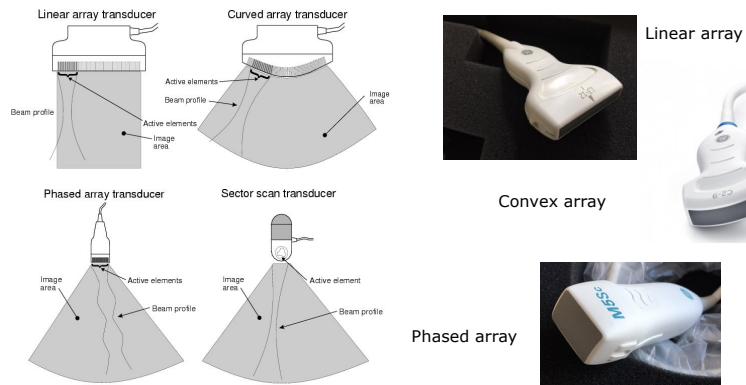
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Medical Ultrasound: Imaging



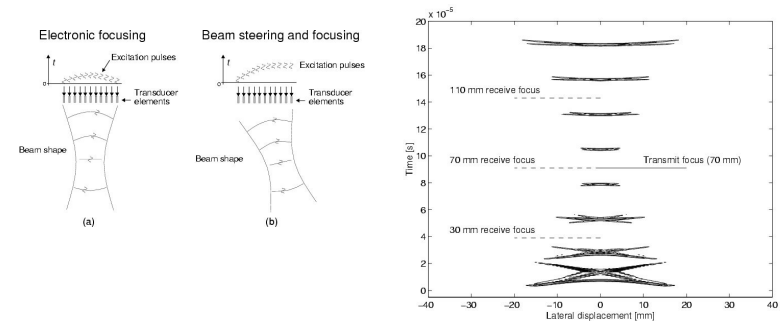
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Different array transducers and imaging types




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Transducers and focusing



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Signal processing in B-mode system



- Transmit pulse
- Receive and amplify in TGC amplifier
- Sample signal


$$y(t) = r(t) * p(t)$$
- Calculate envelope through Hilbert transform

$$e(n) = \sqrt{y^2(n) + H[y(n)]^2}$$
- Compress dynamic range

$$e_{disp}(n) = 20 \log_{10}(e(n))$$
- Scale to color map
- Make rectangular-to-polar mapping

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Signal processing in a B-mode system (Exercise 1)





1 cm between markers
(15 x 15 cm)

This is exercise 1
Monday September 9

B-mode image of right liver lobe and kidney

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Discussion assignment for Thursday

- Design an ultrasound B-mode system
- Assume that a system can penetrate 300 wavelengths
- It should penetrate down to 10 cm in a liver
 - What is the largest pulse repetition frequency possible?
 - What is the highest possible transducer center frequency?
 - What is the axial resolution?
 - What is the lateral resolution for an F-number of 2?

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Summary of today

- Practical details of course
- History of ultrasound
- Basic ultrasound
- Content of exercise 1
- For next time
 - Download and print book from DTU Learn
 - Read chapter 1 and 2, page 1-24 and look at your signal processing books – remember quiz questions
 - Make the discussion assignment
 - We will discuss Chapter 2
 - What are the key parameters of ultrasound?
 - Ultrasound propagation, intensity, reflection, and scattering
 - Next discussion Thursday, 9-12 on these topics
 - Read and prepare questions and discussion for exercise 1
 - Prepare for signal processing quiz

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